AD-A048 803

ROCKWELL INTERNATIONAL ANAHEIM CA ELECTRONIC DEVICES DIV F/6 9/5
AN ELECTRICAL SURGE ARRESTOR (ESA) MODEL FOR COMPUTER-AIDED DES--ETC(U)
NOV 77 C T KLEINER
X77-1102/501

UNCLASSIFIED













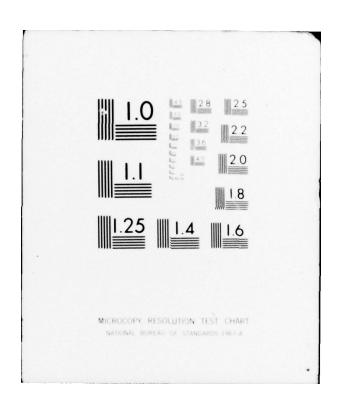








END DATE FILMED 2 -78 DDC







technical information from ...

OBC FILE COPY



DISTRIBUTION STATEMENT A

Approved for public release; Eistribution Unlimited

**Rockwell International** 



AN ELECTRICAL SURGE ARRESTOR (ESA) MODEL FOR COMPUTER-AIDED DESIGN AND EVALUATION

2 Nov 2 1077

By

C. T./Kleiner

Presented to:

Presented at the

Annual Asilomar Conference on

Circuits, Systems and Computers

(14) X77-1102/501

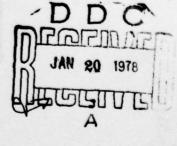
THE DISTRIBUTION OF THIS REPORT
IS UNLIMITED

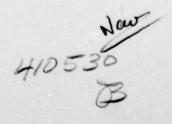


# **Rockwell International**

Electronics Research Center Electronic Devices Division

3370 Miraloma Avenue P.O. Box 4182 Anaheim, California 92803





# AN ELECTRICAL SURGE ARRESTOR (ESA) MODEL FOR COMPUTER-AIDED DESIGN AND EVALUATION

by

C. T. Kleiner Rockwell International Electronic Devices Division Anaheim, California

#### I. Summary

Electrical Surge Arrestors (ESA's) are widely used to protect susceptible electrical and electronic components sub-systems and systems from the potentially damaging effects of lightning, static discharge, Electromagnetic interference and the Electromagnetic pulse arising from potential nuclear weapon detonations. ESA's are very non-linear devices when operating near or above the DC breakdown potential. The ESA model to be described accounts for a significant number of nonlinear effects including (1) streamer formation. (2) plasma conductivity. (3) glow region. (4) are extinguishing. (5) high frequency oscillations. (6) Thermionic effects, and (7) heating and heat dissipation to the surrounding medium. The model is illustrated in Figure 1 with a corresponding definition for each parameter in the model.

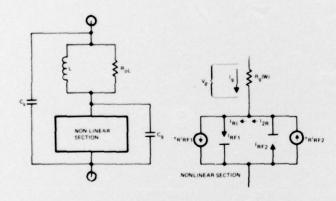


Figure 1. Electrical Surge Arrestor (ESA) Model

## II. Model Parameters and Equations

Figure 1 illustrates the equivalent circuit for the Electrical Surge Arrestor model. The linear portion of the model is defined by the L, R<sub>pL</sub>, C<sub>g</sub> and C<sub>s</sub> elements. The nonlinear portion of the model is also illustrated and basically represents the complex reaction of initial streamer/ arc formation followed by plasma formation and includes the Thermionic potential observed during the ON or conduction phase of ESA operation. The various model parameters, nonlinear equations which utilize the parameters will be defined and illustrated by model application and comparison to test results. The various test circuits are also shown for the benefit of other investigators wishing to characterize ESA's or spark gaps in a manner described herein.

Definition of Model Parameters and Equations

#### 1. Linear Section

L = Lead Inductance (usually in nano henries)

R<sub>pL</sub> = Flux loss ("Q") associated with L (usually in K ohms)

C<sub>S</sub> = Stray Capacitance (reflected capacitance at the ESA terminals from all other sources, leads, etc.)

C<sub>f</sub> = Gap Capacitance (measured or calculated for the Gap)

#### 2. Nonlinear Section

(a) Rg = A nonlinear resistor dependent on the energy being dissipated within the gap and transferred to the surrounding medium

Equations:

$$R_{g} = \frac{K_{1}}{W} \tag{1}$$

$$W = W_{IN} - W_{OUT}$$
 (2)

$$W_{IN} = \int \left[ \frac{V_g^2}{R_{gn-1}} \right] dt$$
 (3)

$$W_{OUT} = \int \frac{W}{\tau d} dt \text{ or } \left[ P_{ml} dt_i \right]$$
 (4)

(whichever is less)

where:

R = Instantaneous Resistance of the gap (ohm)

V = Instantaneous Voltage across the gap (volts)

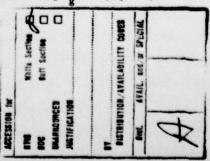
I = Instantaneous Current through the gap (amps)

W = Instantaneous Energy in the gap (joules)

 $W_{IN}$  = Instantaneous Energy generated as input to the gap (joules)

W<sub>OUT</sub> = Instantaneous Energy removed from the gap to the surrounding medium (joules)

 $K_1$  = Scale factor relating  $R_{\sigma}$  to W ( $\Omega$ -joules)



P<sub>m1</sub> = Maximum instantaneous power lost to the surrounding medium (watts)

Td = Dissipation time constant (an average thermal time constant for establishing the rate at which heat energy (joules) is dissipated to the surrounding medium) (sec)

R<sub>gmax</sub> = Maximum resistance of the air gap (ohms)

R<sub>gmin</sub> = Minimum resistance of the air gap (ohms)

Wmin = Minimum energy in the air gap (joules)

V<sub>DB</sub> = Gap breakdown threshold voltage (volts) V<sub>DB</sub> ≈ 100KV/inch in air at STP

τ SF = Time for Streamer Formation (τ SF increases with gap width)

Igmin = Instantaneous value of arc current below which the arc extinguishes.

The following controls are employed:

No. 1 If V<sub>g</sub> ≥ V<sub>DC</sub> and W ≥ 0, then initiate timer at t<sub>o</sub> (time at which the condition for streamer formation has been achieved)

No. 2 At  $t = t_0 + \tau_{SF}$  initiate computation of W and subsequent modification of  $R_g$  (see Figure 2 characteristic curve)

No. 3 Continue to monitor W until W  $\leq$  W<sub>min</sub>. Also monitor R<sub>g</sub> and limit R<sub>g</sub> to R<sub>gmin</sub> by comparing R<sub>g</sub>(W) to R<sub>gmin</sub>

No. 4 Return  $R_g$  to  $R_{gmax}$  when gap is fully extinguished  $I_g \le I_{gmin}$ 

(b) Thermionic Effect = The phenomenon that accounts for the high ON voltages observed in ESA's (over 100 volts), whereby the emitting ESA block effectively becomes a cold cathode, while the collecting ESA block becomes the plate, in what is essentially Thermionic reaction, namely, the plasma creates a junction which is represented mathematically by the following equations:

$$I_{RF1} = I_{S1} (\exp VR/M_1\theta) - 1)$$
 (5)

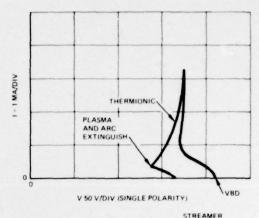
$$I_{RF2} = I_{S2} (\exp - VR/M_2\theta) - 1)$$
 (6)

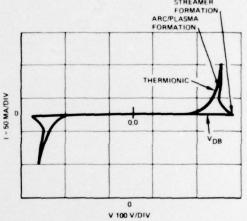
where:

 $V_{R}$  = Thermionic junction potential (volts)

I<sub>S1</sub>, I<sub>S2</sub> = A pseudo-saturation current for the Thermionic Rectifier (and are also functions of temperature and effective plasma area)

M<sub>1</sub>, M<sub>2</sub> = Multiplier for empirical fit (M has a range of 50 to 500 depending on the particular ESA) (non-dimensional)





(b) LOW FREQUENCY I VS V CHARACTERISTICS OF (a)

Figure 2. Non-Linear Section of ESA Model and Low Frequency I (V) Characteristics

In addition, there is a slight tendency for these "Thermionic Rectifiers" to "store" charge similar to a semiconductor rectifier, hence, the net current in each Thermionic Rectifier is formulated as follows:

$$I_{R1} = I_{RF1} + \tau_R \dot{I}_{RF1}$$
 (7)

$$I_{R2} = I_{RF2} + \tau_R \dot{I}_{RF2}$$
 (8)

where:

TR = Thermionic electron recombination time (which is believed to be on the order of a few nanoseconds)

$$\theta = kT/q = .026 @ 27^{\circ}C \ (T \text{ is set } @ 300^{\circ}K)$$
 (9)

A set of typical ESA model data is shown in Table I.

Using non-linear model shown in Figure 1, and the data shown in Table I, it was possible to analytically obtain I versus V characteristics showing the extremely non-linear behavior of the gap for (1) Streamer, (2) Arc/plasma, and (3) Thermionic formation including extinguishing of the arc. This is shown in Figure 2.

Table I. Example of ESA Data

	Parameter	Value	Units
Linear Section	L	130	nh
	$R_{pL}$	2500	ohm s
	Cg	3.18	pfd
	$c_s$	1	pfd
Nonlinear Rg Section	к,	2/-3	ohm-Joules
	P <sub>m1</sub>	1500	Watts
	<sup>⊤</sup> d	.1	usec
	Rgmax	1/+12	ohms
	Rgmin	.1	ohms
	Wmin	1/-10	Joules
	$v_{DB}$	185	Volts
	<sup>⊤</sup> SF	1	nsec
	<sup>I</sup> gmin	5	ma
Thermionic	I <sub>s</sub>	1	ua
	M	500	-
	$^{T}\mathbf{R}$	.1	nsec

#### III. ESA CHARACTERIZATION

Several types of ESA's were modeled and characterized (Audio, Power and Antenna ESA's) for both the linear and non-linear components of the model.

The linear characteristics can be obtained quite readily by using a network analyzer and solving for the values of L,  $C_S$ ,  $C_g$ , and  $R_{pL}$ . The result for an Audio ESA is shown in Figure 3.

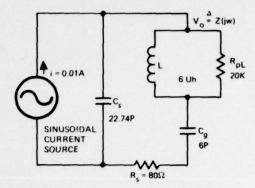
The nonlinear characteristics are considerably more difficult to obtain.

The following tests were conducted to obtain the nonlinear characteristics:

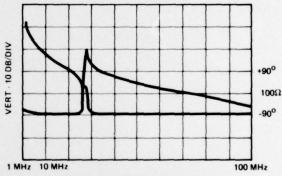
#### 1. Sawtooth Oscillator Test

The first test that can be performed is shown in Figure 4 where the ESA is used as the nonlinear element which produces a sawtooth oscillation. Resistor, R<sub>1</sub>, must be sufficiently large so that the 'holding current' wi!' not sustain a very low electron leakage and prevent oscillation. This determines one of the critical parameters, namely, the minimum power to sustain the arc. This may not be the minimum power required to completely describe the interaction of the plasma with the surrounding medium however. The dynamic resistance of the arc can appear quite high even though the capacitor, C<sub>1</sub> is a very low impedance source at the switch point and hence, would be expected to discharge rapidly giving rise to a high current pulse through the ESA; this is not the case for this or other ESA's. The reason for this apparent high discharge impedance in this

sawtooth oscillator configuration is postulated to be due to



(a) SMALL SIGNAL EQUIVALENT CIRCUIT (FIGURE 1 LINEAR SECTION)



HOR = 1 MHz THROUGH 100 MHz

(b) LABORATORY TEST RESULTS (USING HP NETWORK ANALYSER)

Figure 3. Small Signal Equivalent Circuit for Audio ESA (Below Breakdown) and Laboratory Test Response

the relatively high resistance of R<sub>gap</sub> and the relatively high impedance of the onset of the Thermionic conduction

 $\frac{M_{\theta}}{I_{gap}}$ 

#### 2. Fast Rise Time Test

When the ESA is subject to a high voltage, fast risetime input, two characteristics become apparent. First, the firing potential increases and second, the ON voltage is only somewhat higher than during the sawtooth operation. The dynamic resistance becomes much lower which satisfies the functional relationship between R  $_{gap}$  and  $M_{\theta}/I_{gap}$  (both resistors being inverse to arc current density). The high dv/dt input results in a voltage breakdown vs rise-time characteristics as shown in Figure 5. There are two regions of the curve which are worthy of discussion, Region I shows a fairly gradual increase in apparent gap breakdown with increasing dv/dt. This increase is attributable to the interaction of the arc formation and energy dissipation coupled with the effect of the reactive linear elements (L's and C's) of the ESA. In Region II the apparent breakdown of the ESA vs dv/dt increased more rapidly. This is attributed to the time required for streamer formation. This occurs prior to arc formation. The net effect of this ESA response to very high values of dv/dt (or high frequency) reduces ESA effectiveness for the high frequency components of disturbance.

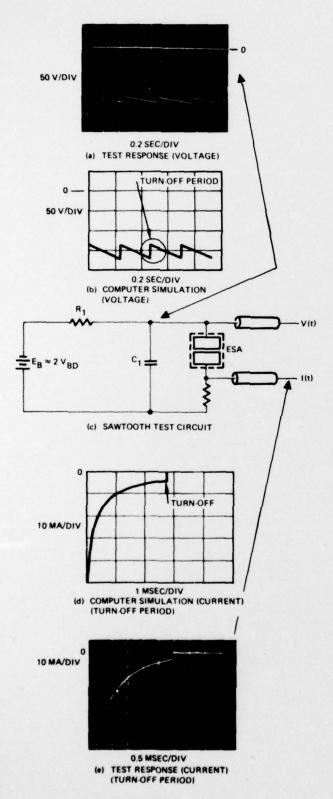
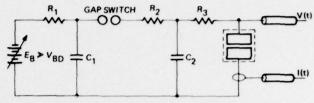
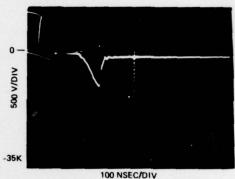


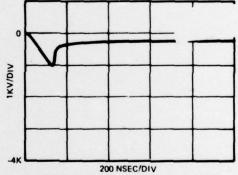
Figure 4. Sawtooth Oscillator Test Results and Comparison to Computer Model Response



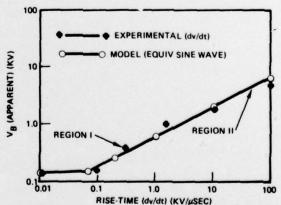
(a) FAST RISE TIME TEST CIRCUIT (R<sub>1</sub> = 1 MEG, C<sub>1</sub> = 0.02 UFD, R<sub>2</sub> = R<sub>3</sub> = 510 $\Omega$ , C<sub>2</sub> VARIED FROM 50 PFD THROUGH 350 PFD)



(b) REST RESULTS (VOLTAGE)



(c) COMPUTER MODEL RESPONSE (VOLTAGE)



(d) PLOT OF INCREASED BREAKDOWN VOLTAGE V<sub>B</sub> (APPARENT) VS RISE TIME (dv/dt) OR EQUIVALENT FREQUENCY f

Figure 5. Characterization of Increase in Apparent Voltage Breakdown (or Overshoot) vs Rise Time Test Circuit. Results and Plot of  $$V_{\rm B}$$  vs dv/dt

#### 3. Damped Sine Wave Test

In practice a damped sinewave is frequently used to characterize component and/or subsystem response to Electrical Surges. As a result, the ESA and corresponding model were also characterized using various damped sinewave input stimulus. The result of this test and model simulation as illustrated in Figure 6. Note that the ESA's can open after the initial shorting if the sustaining energy is insufficient to cause the arc to sustain. This is particularly true for lower frequencies (-1 MHz and below) and higher impedance (-1 KM) sources.

#### IV. Example Computer Coding for the ESA Models Using SYSCAP II

The SYSCAP II program was used to perform several studies involving the spark gaps and surge arrestors discussed in Section III. This section will illustrate how some of these models were programmed using the SYSCAP II ALCAP and TRACAP subprograms.

ALCAP: The ALCAP (A. C. Linear Computer Analysis Program) was used to model the linear network shown in Figure 3. Figure 7 illustrates the coding list used to obtain the results shown in Figure 3. In addition to the amplitude and phase vs frequency response, the ALCAP program was also used to determine the sensitivity of the amplitude and phase response to component tolerance at various frequencies. This capability of the program was very useful in characterizing the networks since it identified which elements were the most critical. It showed that L and C were very critical around resonance while R pL and C were not as sensitive.

TRACAP: The TRACAP (TRAnsient Computer Analysis Program) was used to model the combined linear and non-linear model shown in Figure 1. Figure 8 illustrates an example of TRACAP coding used to obtain the non-linear I(v) characteristics (as shown in Figure 2). It should be noted that there is a significant negative resistance region which is characteristic of spark gaps which has been very difficult to model in the past but posed no significant problems using the TRACAP code due to the conservative convergence algorithms that have been used.

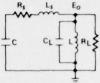
Another example of TRACAP application for ESA modeling is illustrated in Figure 9 where a damped sine-wave stimulus simulates a potential surge disturbance. The results are compared to test data shown in Figure 10. In this case two functions are used, namely FUNC 1 to characterize the ESA resistance R<sub>g</sub>(W) and FUNC 2 to generate the exponentially damped sine wave;

$$f_2 = A \epsilon^{-(t/t)} \sin(wt)$$
.

These examples have been given so that scientists and engineers who are interested in this type of model (surge protection analysis/design) can readily avail themselves of this capability via the SYSCAP program.

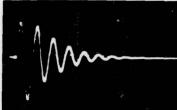
### V. Conclusions

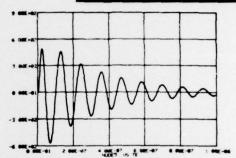
The ESA model presented in this paper is relatively easy to use (in an appropriate computer program such as SYSCAP II) and permits a detailed evaluation spark gap protection to a variety of electrical surge stimulus. The model accounts for the extremely nonlinear behavior of the ESA gap including intermittent firing, variation in ON impedance and other related phenomenon. Examples of model application demonstrate the behavior of the model in the linear and non-linear regions.



(a) EQUIVALENT CIRCUIT FOR DAMPED SINEWAVE PULSER
(Rs INCLUDES NONLINEAR GAP RESISTANCE)

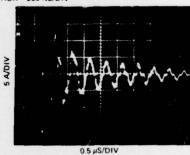




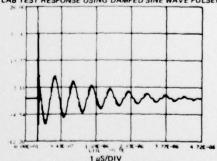


EXAMPLE OF PULSER MODEL (C/R) USING SIMPLE EQUIVALENT CIRCUIT LAB TEST RESULTS

(c) EQUIV CIRCUIT RESPONSE (PDP8e) VERT = 300 V/DIV HOR = 200 NS/DIV



(d) LAB TEST RESPONSE USING DAMPED SINE WAVE PULSER



(e) ESA MODEL RESPONSE (INCLUDING SHORT INDUCTANCE LOOP RINGING) (TEKTRONIX 4010)

Figure 6. Comparison of ESA Lab Tests (Damped Sinewaye) and ESA Model Response (Tektronix 4010 Display)

# BEST AVAILABLE COPY

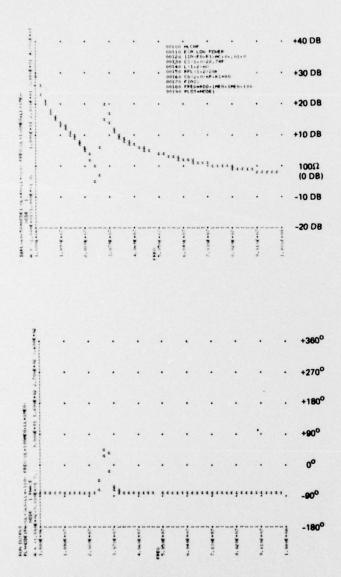


Figure 7. SYSCAP II (ALCAP) Coding and Amplitude/Phase Response Using a TI Silent 700 Terminal

## VI. References

 SYSCAP II User Information Manual (Publication No. 76070600), Available through CDC Cybernet Data Services Publications, P.O. Box O. HQW05F, Minneapolis, MN 55440

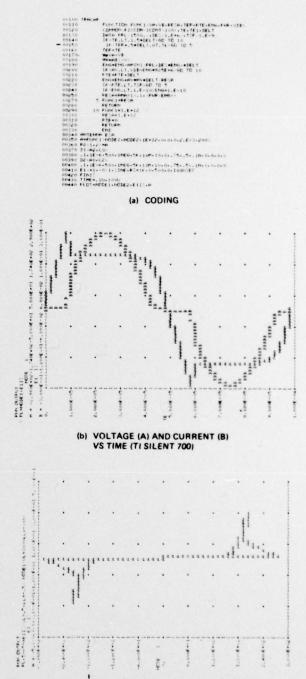
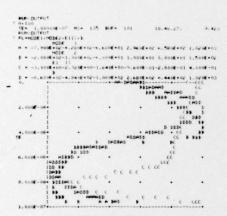


Figure 8. Illustration of Interactive SYSCAP II (TRACAP)
Coding and Response Using a TI 700 Terminal

(c) PLOT OF I VS V (NODE 1)



#### (a) CODING



#### (b) PLOT OF NODE 1, 2, CURRENT (E1IS) THROUGH ESA AND GAP RESISTANCE

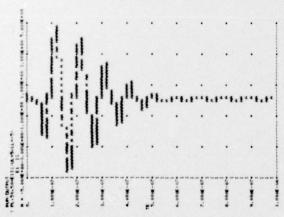
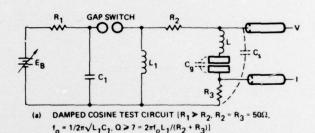
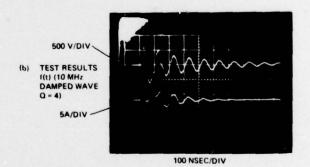


Figure 9. Illustration of Interactive SYSCAP II (TRACAP) Coding and Response for a Damped Sinewave Input

(c) CURRENT VS TIME

BEST AVAILABLE COPY





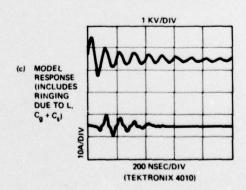


Figure 10. Test Circuit and Response Comparison for a Damped Sinewave